# Investigating Dimensionality by means of Mokken Analysis and Confirmatory Factor Analysis

Ingo W. Nader, Ulrich S. Tran, Patricia Baranyai, Martin Voracek University of Vienna ingo.nader@univie.ac.at

Psychoco 2012: International Workshop on Psychometric Computing University of Innsbruck, Austria February 10, 2012



# Mokken Analysis

# A lot of favorable properties:

- ► has been around for some time (Mokken, 1971; Sijtsma & Molenaar, 2002)
- ▶ in the framework of nonparametric item response theory
- ▶ can be applied to dichotomous or polytomous (ordinal) data
- empirically testable assumptions

## But hardly ever used:

- still rather unknown (except in the Netherlands)
- sounds complicated item response functions of unknown form?
- results not easily comparable to "standard research"
- ▶ no (commonly known) benchmarks for model fit

Investigating Dimensionality with Mokken Analysis and CFA

Nader et al.

ntroduction

Investigating Dimensionality

Mokken Analysis

Practical Example

Attitudes Toward Suicide

Mokken Analysis Confirmatory Factor

Discussion

Conclusion

1 / 27

Investigating
Dimensionality
with
Mokken Analysis
and CFA

Nader et al.

ntroduction

Mokken Analysis
Automated Item Selection

Practical Example

Results Mokken Analysis

Confirmatory Facto Analysis

Discussion

Conclusion

# Investigating Dimensionality

#### Most common methods:

- Principal Component Analysis (PCA)
- ► Exploratory Factor Analysis (EFA)
- Confirmatory Factor Analysis (CFA)

#### Less common methods:

- DIMTEST (Stout, Nandakumar, Junker, Chang, & Steidinger, 1992)
- ► DETECT (Zhang & Stout, 1999)
- ► Mokken Analysis (Mokken, 1971; Sijtsma & Molenaar, 2002)

# Mokken Analysis

# Has already been used conjointly with PCA:

- unsurprisingly, by researchers from the Netherlands (Wismeijer, Sijtsma, van Assen, & Vingerhoets, 2008)
- combined use was found to be beneficial in terms of these methods complementing each other

# Can also be used conjointly with CFA:

- ► CFA offers well-established benchmarks to assess the fit of factor models (e.g., Hu & Bentler, 1999)
- can make results comparable to prior research
- Mokken Analysis offers an "additional dimension" over (exploratory/confirmatory) factor analysis

Investigating Dimensionality with Mokken Analysis

and CFA

Introduction

Investigating Dimensionalit

Automated Item Selection

Practical Example

Attitudes Toward Suici

Mokken Analysis

Confirmatory Facto

Discussion

Conclusion

2 / 27

Investigating
Dimensionality
with
Mokken Analysis

Nader et al

Introductio

Mokken Analysis

Procedure

Practical Example
Attitudes Toward Suicide

Results

Mokken Analysis

Confirmatory Factor Analysis

Conclusion

10140101010100

# Mokken Analysis

- ▶ based on the Monotone Homogeneity Model (MHM; Mokken & Lewis, 1982; Sijtsma & Molenaar, 2002)
- assumptions:
  - unidimensional latent trait(s)
  - monotonicity
  - local independence of responses
- ▶ Mokken Analysis can be used to select items to scales in order to satisfy the MHM
- by calculating scalability coefficients
  - $ightharpoonup H_{ii}$  for item pairs
  - $ightharpoonup H_i$  for single items in relation to their common scale
  - H for the complete scale
- and using an automated item selection procedure

# Practical Example

Attitudes Toward Suicide Scale (Eskin, 2004)

measures different factors (EFA):

- acceptability of suicide
- suicide as a sign of mental illness
- ▶ the belief that persons who commit suicide will be *punished* after death
- ▶ the opinion that suicidal people should communicate their problems
- ▶ the intention to hide past suicidal behavior
- ▶ the opinion that suicide should be discussed and reported openly among friends or in the news

and maybe

▶ the view of *suicide as a solution* to one's problems

as found by another study using EFA (Eskin, Voracek, Stieger, & Altinyazar, 2011).

Investigating Dimensionality Mokken Analysis

and CFA Nader et al.

Mokken Analysis

5 / 27

Investigating Dimensionality Mokken Analysis and CFA

Attitudes Toward Suicide

# Automated Item Selection Procedure

- 1. select the two items to form a scale
  - ▶ that have the highest pairwise scalability coefficient H<sub>ii</sub>
  - which has to be higher than a user-specified minimum value c (scalability criterion)
- 2. from the remaining items, select the item
  - that correlates positively with all items already in the scale
  - that has a pairwise scalability coefficient  $H_{ii} > c$  with all items in the scale
  - ▶ that maximizes the scale's scalability coefficient H
- 3. repeat step 2 until no item satisfies these conditions
- 4. start at step 1 to construct a second/third/...scale
- repeat this procedure for increasing scalability criteria c
- resulting in an increasing number of more and more clear-cut scales (and more unscalable items)
- ▶ thereby revealing the dimensionality of the questionnaire



6 / 27

# Attitudes Toward Suicide

## Practical/clinical relevance

Especially the factor acceptability of suicide is important for suicide prevention, as higher acceptability ...

- moderates the relationship between hopelessness and suicidal ideation (in men; Gibb, Andover, & Beach, 2006)
- ▶ is linked to increased planning of suicidal actions in adolescents (Joe, Romer, & Jamieson, 2007)
- may be associated with higher suicide rates (Salander Renberg, Hjelmeland, & Koposov, 2008)
- ▶ although findings remain debated (Beautrais, Horwood, & Fergusson, 2004; Salander Renberg et al., 2008)

Investigating Mokken Analysis and CFA

Investigating

Dimensionality

Mokken Analysis

and CFA

Nader et al.

Automated Item Selection

# 6 or 7 Factors?

### To resolve this issue:

- ► Mokken Scaling
  - ▶ to investigate dimensionality non-parametrically
  - ▶ using R 2.14.1 (R Development Core Team, 2011)
  - ▶ and package mokken Version 2.6 (van der Ark, 2007)
- ► CFA
  - ▶ to quantify the fit of the models
  - ▶ using lavaan Version 0.4-10 (Rosseel, 2011)
  - ▶ and MPlus 6.1 (Muthén & Muthén, 2008)

## Sample:

- ▶ N = 571 German-speaking volunteers (41% men)
- subjects with missings omitted
- ▶ mean age 30 years (SD = 12.8 years)

4 D > 4 B > 4 E > 0 E

c = .10 to .15

- 1. Someone who has gone bankrupt has the right to kill him/herself
- Someone who is tired of living has the right to kill him/herself
- Someone who dishonored his/her family has the right to kill him/herself
- 4. Someone suffering from an incurable illness has the right to kill him/herself.
- 5. Suicide can be a solution to some problems.
- 6. Suicide can be the only way out of life's problems.
- 7. People have the right to kill themselves.
- 8. Killing oneself by committing suicide is a right behavior.
- 9. People who attempt suicide are mentally ill.
- 10. People who kill themselves by committing suicide are mentally ill.
- 11. People who think and plan suicide are mentally ill.
- 12. People who attempt suicide are going to be punished in the other world.
- 13. People who kill themselves are going to be punished in the other world.
- 14. People who think and plan suicide are going to be punished in the other world.
- 15. People who kill themselves by committing suicide are sinful.
- 16. There is a life after death.
- 17. A person who [...] plans suicide should tell [...] friends [...
- 18. People should tell their psychological problems to their friends.
- 19. Young people should tell their psychological problems to their parents.
- 20. A young person who thinks and plans suicide should tell this to his/her parents.
- 21. Families whose daughter/son attempts suicide should hide this from their neighbors.
- 22. Families who lose a daughter/son from suicide should hide this from their neighbors.

4 D > 4 A >

- 23. Suicide news should be written openly in the newspapers.
- 24. The matter of suicide should be discussed openly among friends.
- ▶ 4 scales now (open reporting of suicides splits off)

Investigating
Dimensionality
with

Mokken Analysis and CFA Nader et al.

Introduction

Investigating Dimensionalit

Mokken Analysis

Automated Item Selectio

Practical Example

Attitudes Toward Suicide

December

Confirmation Factor

Analysis

D1500551011

Conclusion

9 / 27

Investigating
Dimensionality
with
Mokken Analysis

Nader et al.

Introduction

Investigating Dimensionality
Mokken Analysis

Automated Item Selection Procedure

Practical Example
Attitudes Toward Suicide

Results

Mokken Analysis

Confirmatory Factor

Diaguasian

Conclusion

c = .00 to .05

- 1. Someone who has gone bankrupt has the right to kill him/herself
- 2. Someone who is tired of living has the right to kill him/herself.
- Someone who dishonored his/her family has the right to kill him/herself.
- 4. Someone suffering from an incurable illness has the right to kill him/herself.
- 5. Suicide can be a solution to some problems.
- 6. Suicide can be the only way out of life's problems.
- 7. People have the right to kill themselves.
- 8. Killing oneself by committing suicide is a right behavior
- 9. People who attempt suicide are mentally ill.
- 10. People who kill themselves by committing suicide are mentally ill
- 11. People who think and plan suicide are mentally ill.
- 12. People who attempt suicide are going to be punished in the other world.
- 13. People who kill themselves are going to be punished in the other world.
- 14. People who think and plan suicide are going to be punished in the other world.
- 15. People who kill themselves by committing suicide are sinful.
- 16. There is a life after death.
- 17. A person who [...] plans suicide should tell [...] friends [...
- 18. People should tell their psychological problems to their friends.
- 19. Young people should tell their psychological problems to their parents.
- 20. A young person who thinks and plans suicide should tell this to his/her parents.

Someone who has gone bankrupt has the right to kill him/herself

People who kill themselves by committing suicide are mentally ill.

People who kill themselves by committing suicide are sinful.

A person who [...] plans suicide should tell [...] friends [...]

Suicide news should be written openly in the newspapers.

People should tell their psychological problems to their friends.

People who attempt suicide are going to be punished in the other world.

People who kill themselves are going to be punished in the other world.

Young people should tell their psychological problems to their parents.

People who think and plan suicide are going to be punished in the other world.

A young person who thinks and plans suicide should tell this to his/her parents.

Families whose daughter/son attempts suicide should hide this from their neighbors.

Families who lose a daughter/son from suicide should hide this from their neighbors.

Someone who is tired of living has the right to kill him/herself.

Someone who dishonored his/her family has the right to kill him/herself.

Someone suffering from an incurable illness has the right to kill him/herself.

- 21. Families whose daughter/son attempts suicide should hide this from their neighbors.
- 22. Families who lose a daughter/son from suicide should hide this from their neighbors.
- 23. Suicide news should be written openly in the newspapers.
- 24. The matter of suicide should be discussed openly among friends
- > 3 scales to begin with

c = .20

There is a life after death.

Suicide can be a solution to some problems.

People who attempt suicide are mentally ill.

Suicide can be the only way out of life's problems. People have the right to kill themselves.

People who think and plan suicide are mentally ill.

Killing oneself by committing suicide is a right behavior

10 / 27

Investigating

Dimensionality

with

Mokken Analysis

and CFA

Nader et al.

Mokken Analysis

Investigating
Dimensionality
with
Mokken Analysis

and CFA Nader et al

Introduction

Mokken Analysis

Practical Example

Attitudes Toward Suice

Mokken Analysis

Confirmatory Factor

Analysis

Conclusion

The matter of suicide should be discussed openly among friends.
 4 scales, all are combinations of the six-factor solution (Eskin, 2004)

scale open reporting not a seperate scale here (unstable scale?)

11.

12.

13.

14.

15.

17.

18.

19.

20.

21.

#### c = .25

1.	Someone who has gone bankrupt has the right to kill him/herself.
2.	Someone who is tired of living has the right to kill him/herself.
3.	Someone who dishonored his/her family has the right to kill him/herself.
4.	Someone suffering from an incurable illness has the right to kill him/herself.
5.	Suicide can be a solution to some problems.
6.	Suicide can be the only way out of life's problems.
7.	People have the right to kill themselves.
8.	Killing oneself by committing suicide is a right behavior.
9.	People who attempt suicide are mentally ill.
10.	People who kill themselves by committing suicide are mentally ill.
11.	People who think and plan suicide are mentally ill.
12.	People who attempt suicide are going to be punished in the other world.
13.	People who kill themselves are going to be punished in the other world.
14.	People who think and plan suicide are going to be punished in the other world.
15.	People who kill themselves by committing suicide are sinful.
16.	There is a life after death.
17.	A person who [] plans suicide should tell [] friends []
18.	People should tell their psychological problems to their friends.
19.	Young people should tell their psychological problems to their parents.
20.	A young person who thinks and plans suicide should tell this to his/her parents.
21.	Families whose daughter/son attempts suicide should hide this from their neighbors.
22.	Families who lose a daughter/son from suicide should hide this from their neighbors.

Suicide news should be written openly in the newspapers.

The matter of suicide should be discussed openly among friends.

4 D > 4 D >

c - 35 to 45

	c = .55  to  .45
1.	Someone who has gone bankrupt has the right to kill him/herself.
2.	Someone who is tired of living has the right to kill him/herself.
3.	Someone who dishonored his/her family has the right to kill him/herself.
4.	Someone suffering from an incurable illness has the right to kill him/herself.
5.	Suicide can be a solution to some problems.
6.	Suicide can be the only way out of life's problems.
7.	People have the right to kill themselves.
8.	Killing oneself by committing suicide is a right behavior.
9.	People who attempt suicide are mentally ill.
10.	People who kill themselves by committing suicide are mentally ill.
11.	People who think and plan suicide are mentally ill.
12.	People who attempt suicide are going to be punished in the other world.
13.	People who kill themselves are going to be punished in the other world.
14.	People who think and plan suicide are going to be punished in the other world.
15.	People who kill themselves by committing suicide are sinful.
16.	There is a life after death.
17.	A person who [] plans suicide should tell [] friends []
18.	People should tell their psychological problems to their friends.
19.	Young people should tell their psychological problems to their parents.
20.	A young person who thinks and plans suicide should tell this to his/her parents.
21.	Families whose daughter/son attempts suicide should hide this from their neighbors.
22.	Families who lose a daughter/son from suicide should hide this from their neighbors.
23.	Suicide news should be written openly in the newspapers

The matter of suicide should be discussed openly among friends

factor open reporting of suicide is dropped

Investigating

with

Mokken Analysis

and CFA

Nader et al.

Dimensionality

Mokken Analysis

13 / 27

Investigating Dimensionality with Mokken Analysis and CFA

Nader et al.

Mokken Analysis

c = .30

Someone who has gone bankrupt has the right to kill him/herself. Someone who is tired of living has the right to kill him/herself. Someone who dishonored his/her family has the right to kill him/herself. Someone suffering from an incurable illness has the right to kill him/herself. Suicide can be a solution to some problems. Suicide can be the only way out of life's problems. People have the right to kill themselves. Killing oneself by committing suicide is a right behavior. People who attempt suicide are mentally ill. People who kill themselves by committing suicide are mentally ill 11. People who think and plan suicide are mentally ill Mokken Analysis 12. People who attempt suicide are going to be punished in the other world. 13. People who kill themselves are going to be punished in the other world. 14. People who think and plan suicide are going to be punished in the other world. People who kill themselves by committing suicide are sinful. 15. 16. There is a life after death 17. A person who [...] plans suicide should tell [...] friends [...] 18. People should tell their psychological problems to their friends. 19. Young people should tell their psychological problems to their parents. 20. A young person who thinks and plans suicide should tell this to his/her parents. Families whose daughter/son attempts suicide should hide this from their neighbors. Families who lose a daughter/son from suicide should hide this from their neighbors. Suicide news should be written openly in the newspapers.

matches the six-factor solution found by Eskin (2004)

The matter of suicide should be discussed openly among friends.

except for item 16 (unscalable)

c = .50

4 D > 4 🗗 >

Someone who is tired of living has the right to kill him/herself. Someone who dishonored his/her family has the right to kill him/herself. Someone suffering from an incurable illness has the right to kill him/herself. Suicide can be a solution to some problems. Suicide can be the only way out of life's problems. Killing oneself by committing suicide is a right behavior. People who attempt suicide are mentally ill. People who kill themselves by committing suicide are mentally ill. 11. People who think and plan suicide are mentally ill 12. People who attempt suicide are going to be punished in the other world. People who kill themselves are going to be punished in the other world. 13. 14. People who think and plan suicide are going to be punished in the other world. 15. People who kill themselves by committing suicide are sinful. 16. There is a life after death.

17. A person who [...] plans suicide should tell [...] friends [...] 18. People should tell their psychological problems to their friends.

19. Young people should tell their psychological problems to their parents. 20.

A young person who thinks and plans suicide should tell this to his/her parents. Families whose daughter/son attempts suicide should hide this from their neighbors.

Families who lose a daughter/son from suicide should hide this from their neighbors.

Suicide news should be written openly in the newspapers. The matter of suicide should be discussed openly among friends.

matches the seven-factor solution found by Eskin et al. (2011)

except for excluded items

Investigating Dimensionality with Mokken Analysis and CFA

Nader et al.

14 / 27

Investigating Dimensionality with Mokken Analysis and CFA

Nader et al.

Mokken Analysis

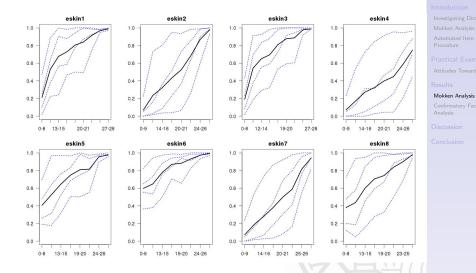
4 D > 4 D > 1 E + O E | Q

#### c = .55

- Someone who has gone bankrupt has the right to kill him/hersel<sup>,</sup>
- Someone who is tired of living has the right to kill him/herself.
- Someone who dishonored his/her family has the right to kill him/herself.
- Someone suffering from an incurable illness has the right to kill him/herself.
- Suicide can be a solution to some problems.
- Suicide can be the only way out of life's problems
- People have the right to kill themselves.
- Killing oneself by committing suicide is a right behavior
- People who attempt suicide are mentally ill.
- People who kill themselves by committing suicide are mentally ill
- People who think and plan suicide are mentally ill.
- 12. People who attempt suicide are going to be punished in the other world.
- 13. People who kill themselves are going to be punished in the other world.
- 14. People who think and plan suicide are going to be punished in the other world.
- 15. People who kill themselves by committing suicide are sinful.
- There is a life after death
- A person who [...] plans suicide should tell [...] friends [..
- People should tell their psychological problems to their friends
- Young people should tell their psychological problems to their parents.
- A young person who thinks and plans suicide should tell this to his/her parents.
- Families whose daughter/son attempts suicide should hide this from their neighbors.
- Families who lose a daughter/son from suicide should hide this from their neighbors.
- Suicide news should be written openly in the newspapers.
- The matter of suicide should be discussed openly among friends
- additional item dropped
- but scales remain essentially unchanged

# Assumption of Monotonicity

**For acceptability** (including the the two "solution"-items 5 and 6):



Investigating Dimensionality Mokken Analysis

and CFA Nader et al.

Mokken Analysis

Investigating

Dimensionality Mokken Analysis

and CFA

# **Dimensionality**

# Dimensionality revealed by:

- increasing the scalability criterion c

- watching how the scales develop
- ▶ to reveal dimensionality of the questionnaire

# 18 / 27

Investigating

Dimensionality

Mokken Analysis

and CFA

Nader et al

Mokken Analysis

## Investigating Mokken Analysis and CFA

#### Mokken Analysis

# Assumption of Monotonicity

# Violations of monotonicity only very minor:

- ▶ no significant violations scales acceptability of suicide, suicide as a sign of mental illness, and hiding suicidal behavior
- one violation for each of the items 14, 18, and 24 (significant at  $\alpha = 5\%$ , but based on 40 pairwise comparisons each)
- ▶ two violations for item 17 (based on 60 pairwise comparisons).
- number of violations appears negligible
- ▶ does not impair the ordering of respondents on the latent trait, i.e., the respective attitude (Wismeijer et al., 2008)

# Confirmatory Factor Analysis

	No.						
	of	Items					
#	Factors	excluded	Split	TLI	CFI	RMSEA	SRMR
1	7	_	no	.881	.901	.082[.077,.087]	.071(.068)
2	6	-	no	.885	.902	.081[.076,.085]	.064(.061)
3	6	16	no	.888	.905	.083[.078,.088]	.062(.060)
4	6	16,17,23,24	yes	.917	.932	.081[.075,.086]	.054(.052)

Note. Split = Splitting the factor *suicide* as a solution from the factor *acceptability* of suicide (yes or no); TLI = Tucker-Lewis index; CFI = comparative fit index; RMSEA = root-mean-square error of approximation; SRMR = standardized root-mean-square residual (lavaan/Mplus); numbers in brackets are 95% confidence intervals for the RMSEA.

# Discussion

- one factor weak (open reporting of suicides, items 23 and 24)
  - ▶ item 23: open reporting in the news (copycat / Werther effects vs. Papageno effect)
  - ▶ item 24: open discussion among friends (experienced as a relief, usually)
- better not use this factor

# $Regarding\ methodology:$

- factor structure revealed by Mokken Analysis
- ightharpoonup "additional dimension" when increasing scalability criterion c
- ▶ allows deeper insights into dimensionality of the scale
- ▶ fit of resulting models can be judged by CFA benchmarks
- ▶ and compared to prior research

Investigating Dimensionality with Mokken Analysis and CFA

Nader et al.

ntroduction
Investigating Dimensiona

Investigating Dimensionality
Mokken Analysis
Automated Item Selection
Procedure

Practical Example
Attitudes Toward Suicide

Confirmatory Factor

Discussion

Conclusion

21 / 27

Investigating Dimensionality with Mokken Analysis and CFA

Nader et a

ntroductio

Mokken Analysis
Automated Item Selection
Procedure

Practical Example
Attitudes Toward Suicide

Results

Confirmatory Factor Analysis

Discussion

Conclusion

Discussion

# Regarding the attitudes toward suicide scale:

- ▶ both (six- and seven-) factor structures from prior research found with Mokken Analysis
- seven-factor solution results from split of the acceptability scale
- suicide as a solution to one's problems:
  - may be regarded as a facet of acceptability
  - or may be treated as a seperate construct (for clear-cut factor structure)
- ▶ hence: six- / seven-factor solution found in prior research maybe due to different importance of this aspect in the two samples

22 / 27

# Conclusion

# Advantages of Mokken Analysis:

- drops unscalable items automatically
- ▶ produces scales (not only data transformations; Wismeijer et al., 2008)
- assumptions empirically testable
- reveals additional insights by increasing the scalability criterion c
- very intuitive

# Advantages of CFA:

- ▶ fit can be judged easily
- well-established benchmarks
- results comparable to prior research
- ⇒ combining both methods combines all advantages

Investigating

Investigating

Dimensionality

Mokken Analysis

and CFA

Nader et al

Discussion

Dimensionality with Mokken Analysis and CFA

Nader et

Introductio

nvestigating Dimensionalit Mokken Analysis

Practical Example

Attitudes Toward Suicide

Results Mokken Analysis

Mokken Analysis

Confirmatory Factor

Discussion

Conclusion

# Outlook

- using the methodology on other questionnaires,
   to construct scales with a more clear-cut factorial structure
- using Mokken Analysis and CFA in cross-validation studies
- making Mokken Analysis more popular?

The state of the s



Fakultät für Psychologie

Thank you.

Ingo Nader
School of Psychology
Department of Psychological Basic Research and Research Methods
University of Vienna
ingo.nader@univie.ac.at

Investigating Dimensionality with

Mokken Analysis and CFA

Nader et al

ntroduction

Mokken Analysis

Practical Example

Attitudes Toward Suicide

25 / 27

Investigating Dimensionality with Mokken Analysis

and CFA

Conclusion

Results

Confirmatory Factor

Discussion

Conclusion

References

Beautrais, A. L., Horwood, L. J., & Fergusson, D. M. (2004). Knowledge and attitudes about suicide in 25-year-olds. Australian and New Zealand Journal of Psychiatry, 38, 260-265. doi:10.1111/j.1440-1614.2004.01334.x

Eskin, M. (2004). The effects of religious versus secular education on suicide ideation and suicidal attitudes in adolescents in Turkey. Social Psychiatry and Psychiatric Epidemiology, 39, 536-542. doi:10.1007/s00127-004-0769-x

Eskin, M., Voracek, M., Stieger, S., & Altinyazar, V. (2011). A cross-cultural investigation of suicidal behavior and attitudes in Austrian and Turkish medical students. Social Psychiatry and Psychiatric Epidemiology, 46, 813-823. doi:10.1007/s00127-010-0254-7

Gibb, B. E., Andover, M. S., & Beach, S. R. H. (2006). Suicidal ideation and attitudes toward suicide. Suicide and Life-Threatening Behavior, 36, 12-18. doi:10.1521/suli.2006.36.1.12

Hu, L. T., & Bentler, P. M. (1999). Cutoff criteria for fit indexes in covariance structure analysis: Conventional criteria versus new alternatives. Structural Equation Modeling: A Multidisciplinary Journal, 6, 1-55. doi:10.1080/10705519909540118

Joe, S., Romer, D., & Jamieson, P. E. (2007). Suicide acceptability is related to suicide planning in US adolescents and young adults. Suicide and Life-Threatening Behavior, 37, 165-178. doi:10.1521/suli.2007.37.2.165

Mokken, R. J. (1971). A theory and procedure of scale analysis. The Hague, the Netherlands: Mouton.

Mokken, R. J., & Lewis, C. (1982). A nonparametric approach to the analysis of dichotomous item responses. Applied Psychological Measurement, 6, 417.

Muthén, L. K., & Muthén, B. O. (2008). Mplus user's guide. Los Angeles, CA: Muthén & Muthén

R Development Core Team. (2011). R: A language and environment for statistical computing. Vienna, Austria: R Foundation for Statistical Computing.

Rosseel. (2011). lavaan: an R package for structural equation modeling and more.

Salander Renberg, E., Hjelmeland, H., & Koposov, R. (2008). Building models for the relationship between attitudes toward suicide and suicidal behavior: Based on data from general population surveys in Sweden, Norway, and Russia. Suicide and Life-Threatening Behavior, 38, 661-675. doi:10.1521/suil.2008.38.6.661

Sijtsma, K., & Molenaar, I. W. (2002). Introduction to nonparametric item response theory. Thousand Oaks, CA: Sage.

Stout, W. F., Nandakumar, R., Junker, B., Chang, H. H., & Steidinger, D. (1992). DIMTEST: A FORTRAN program for assessing dimensionality of binary item responses. *Applied Psychological Measurement*, 16, 236-236. doi:10.1177/014662169201600303

van der Ark, L. A. (2007). Mokken scale analysis in R. Journal of Statistical Software, 20(11). Retrieved from http://www.jstatsoft.org/v20/i11

Wismeijer, A. A. J., Sijtsma, K., van Assen, M. A. L. M., & Vingerhoets, A. J. J. M. (2008). A comparative study of the dimensionality of the self-concealment scale using principal components analysis and Mokken scale analysis. *Journal of Personality Assessment*, 90, 323-334. doi:10.1080/00223890802107875

Zhang, J., & Stout, W. F. (1999). The theoretical DETECT index of dimensionality and its application to approximate simple structure. Psychometrika, 64, 213-249. doi:10.1007/BF02294536

Investigating Dimensionality with

Mokken Analysis and CFA

Nader et al.

Introduction

Investigating Dimensionalit

Automated Item Selection

Practical Example

Attitudes Toward Suid

r (CDUTC)

C C . . . . . . . . . . .

Confirmatory Factor

Conclusion

26 / 2

7 / 27